

# Air-sea scalar transfer – effects of wind and waves on equivalent roughness length

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The 8th International Symposium on Gas Transfer at Water Surfaces

Tuesday 17 May 2022 - Friday 20 May 2022



National Science Foundation  
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# Parameterization of air-sea fluxes of momentum and scalar (temperature, humidity, soluble gases)

1. We parameterize the fluxes using mean wind speed at 10 meter height ( $u_{10}$ ), mean scalar concentrations at 10 meter height ( $\theta_{10}$ ) and at sea surface ( $\theta_0$ ):

$$u_*^2 = C_d u_{10}^2, \quad \theta_* u_* = C_\theta (\theta_{10} - \theta_0) u_{10}$$

2. We assume logarithmic profiles (in height  $z$ ) of mean wind speed ( $u$ ) and mean scalar concentration ( $\theta$ ), under neutral conditions (air temperature = water temperature), inside the constant stress (flux) layer, but above the direct effects of surface waves:

$$\frac{u(z)}{u_*} = \frac{1}{\kappa} \log \frac{z}{z_0}, \quad \frac{\theta(z) - \theta_0}{\theta_*} = \frac{0.74}{\kappa} \log \frac{z}{z_\theta}$$

Then,  $C_d$  and  $C_\theta$  are expressed as:

$$C_d = \left( \frac{1}{\kappa} \log \frac{10}{z_0} \right)^{-2}, \quad C_\theta = \left( \frac{1}{\kappa} \log \frac{10}{z_0} \right)^{-1} \left( \frac{0.74}{\kappa} \log \frac{10}{z_\theta} \right)^{-1}$$

$C_d$  is a function of  $z_0$  alone, but  $C_\theta$  is a function of both  $z_0$  and  $z_\theta$ .

$\tau = \rho_a u_*^2$  : wind stress

$\rho_a$  : air density

$u_*$  : friction velocity

$\theta_* u_*$  : scalar flux

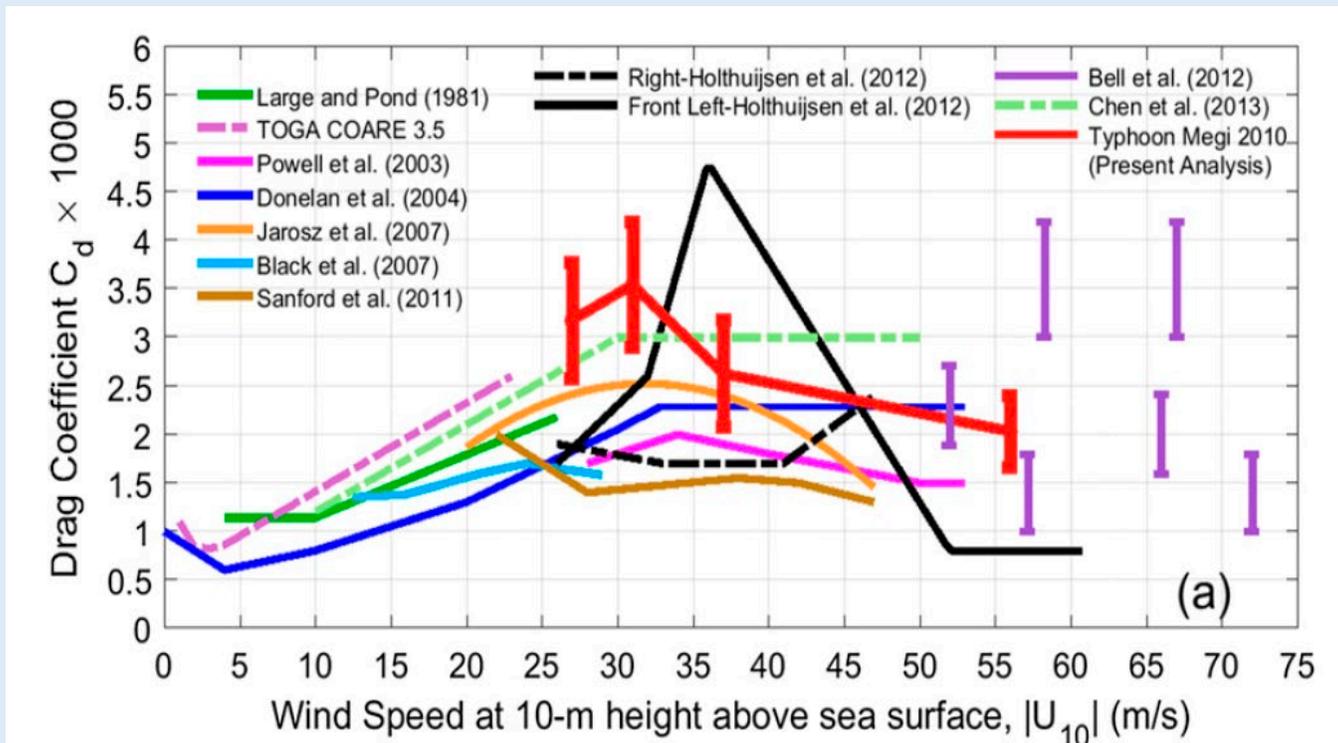
$C_d$  : drag coefficient

$C_\theta$  : scalar transfer coefficient

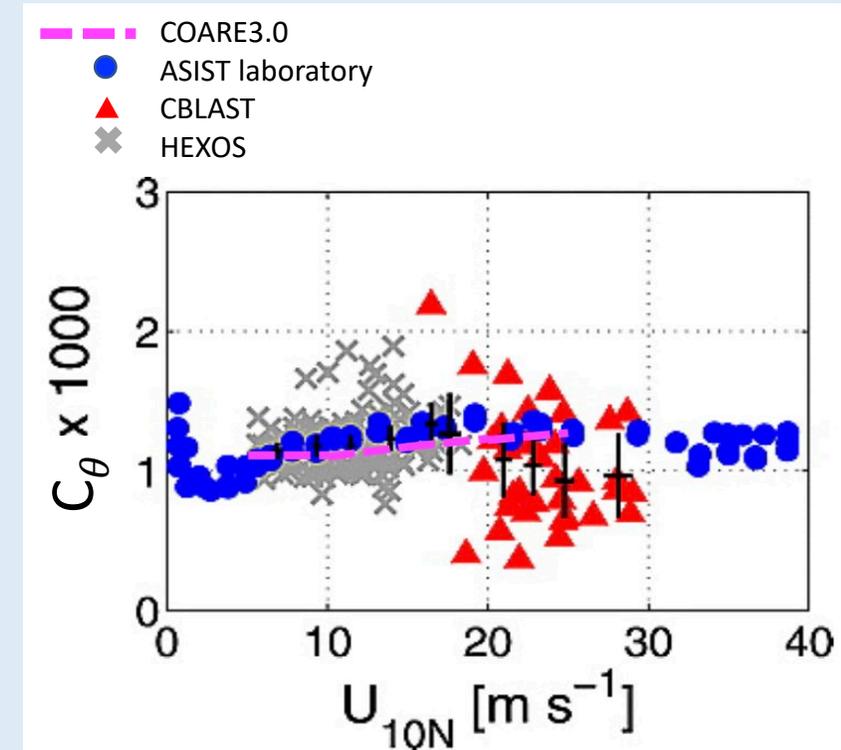
$z_0$  : equivalent surface roughness of wind

$z_\theta$  : equivalent surface roughness of scalar

We know how  $C_d$  and  $C_\theta$  vary with wind speed  $u_{10}$  (on average) quite well, except at very high wind speeds where the uncertainty is large.



Hsu et al. (2017)



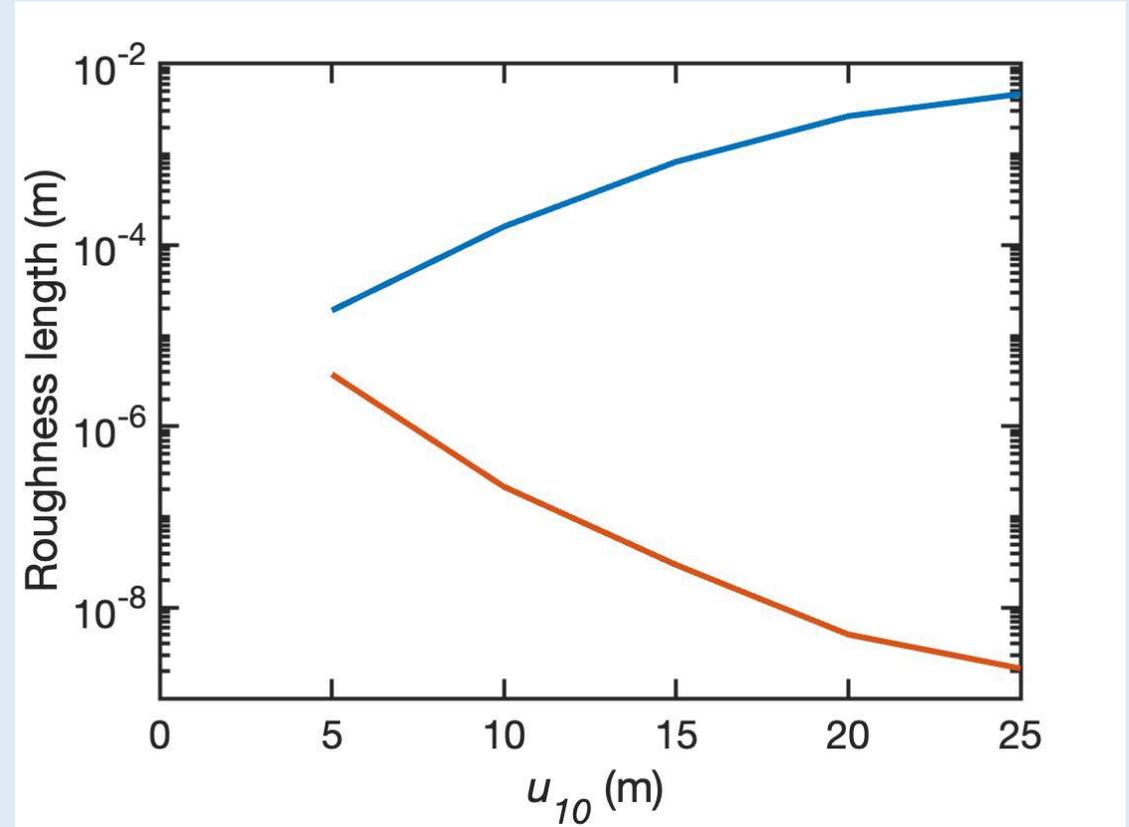
Haus et al. (2010)

Up to wind speed 20 m/s,  $C_d$  rapidly increases but  $C_\theta$  remains almost constant.

Recall that  $C_d$  and  $C_\theta$  are expressed as:

$$C_d = \left( \frac{1}{\kappa} \log \frac{10}{z_0} \right)^{-2}, \quad C_\theta = \left( \frac{1}{\kappa} \log \frac{10}{z_0} \right)^{-1} \left( \frac{0.74}{\kappa} \log \frac{10}{z_\theta} \right)^{-1}$$

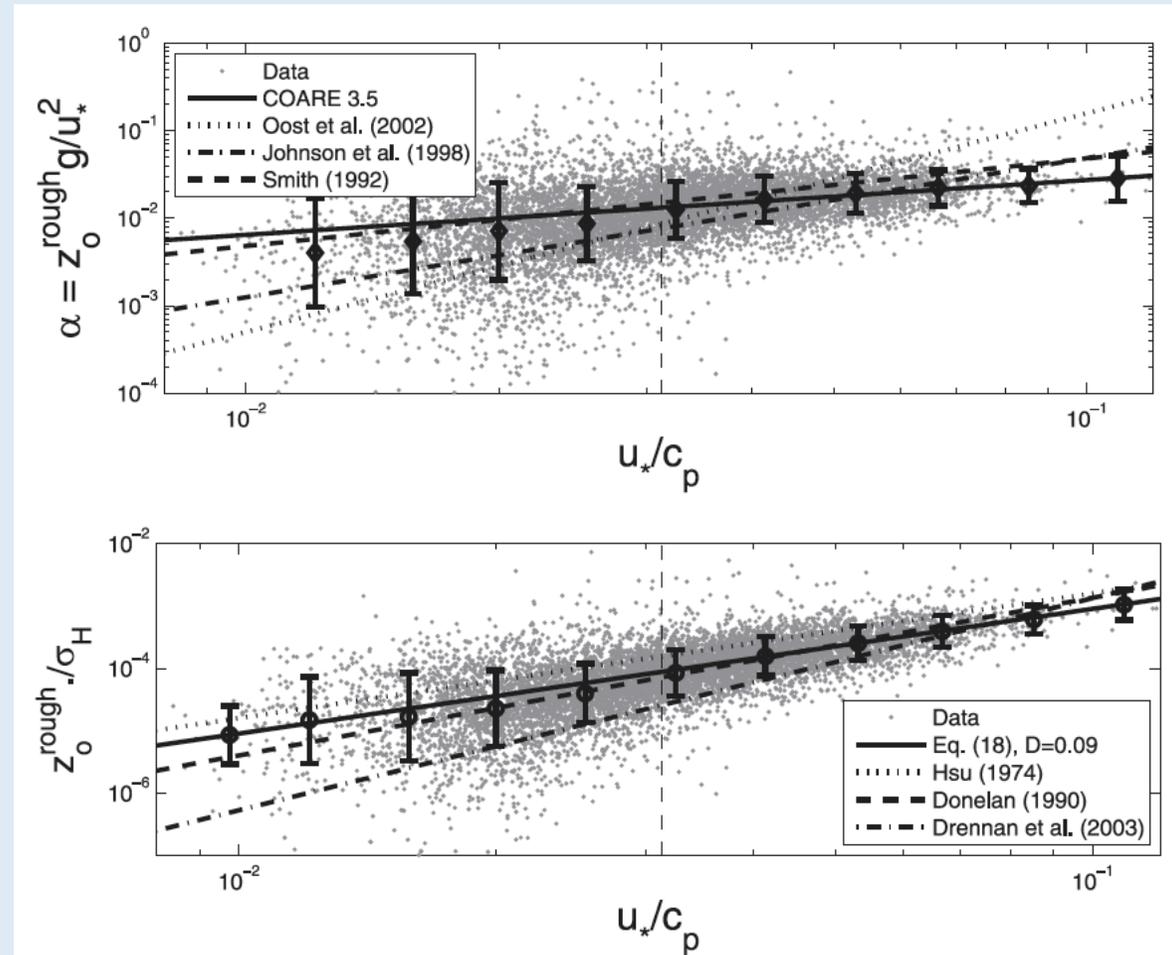
- From COARE3.5  $C_d$  and COARE3.0  $C_\theta$ , we may calculate both  $z_0$  and  $z_\theta$  as functions of  $u_{10}$ .
- $z_0$  rapidly increases with  $u_{10}$ .
- $z_\theta$  rapidly decreases with  $u_{10}$ .
- I will demonstrate how ocean surface waves are responsible for increasing  $z_0$  and decreasing  $z_\theta$ .



$z_0$  (blue) and  $z_\theta$  (red) as functions of  $u_{10}$

# Sea state dependence of $C_d$

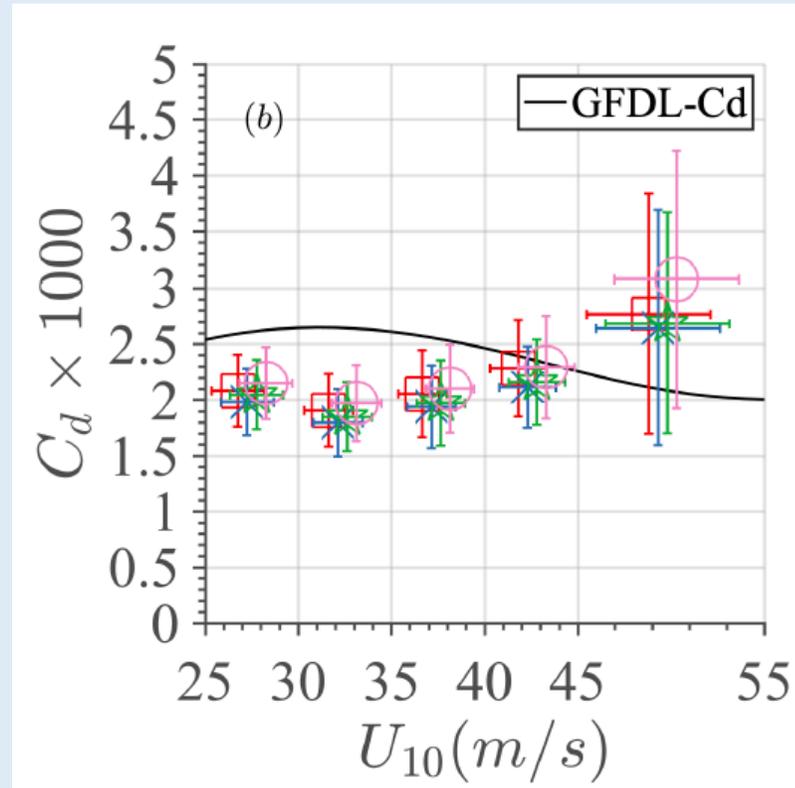
- If ocean surface waves are responsible for increasing  $z_0$ , it is expected that different sea states yield different  $z_0$  (and  $C_d$ ), even if wind speed  $u_{10}$  is the same.
- However, the dependence of  $z_0$  (and  $C_d$ ) on wave parameters (e.g., wave age, wave steepness) is not always clear and not well constrained.



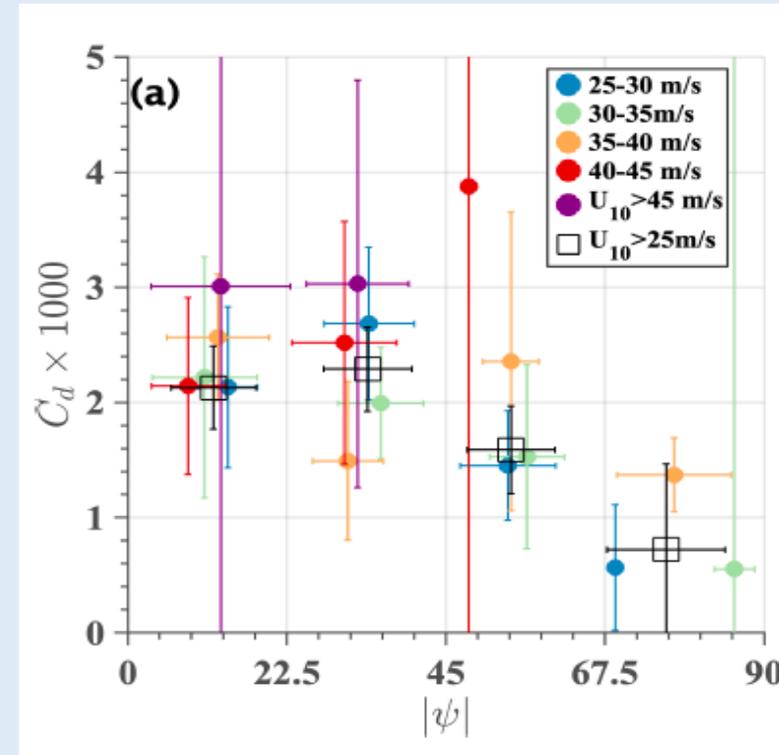
Wave age dependence of normalized roughness  $z_0$  (Edson et al. 2013)

# Sea state dependence of $C_d$

Our recent (observation + model) study suggests  $C_d$  weakly depends on  $u_{10}$  but **strongly depends on sea states under tropical cyclones** (wind speed  $u_{10}$  25-55 m/s) (Zhou et al. 2022).



Wind speed dependence of  $C_d$



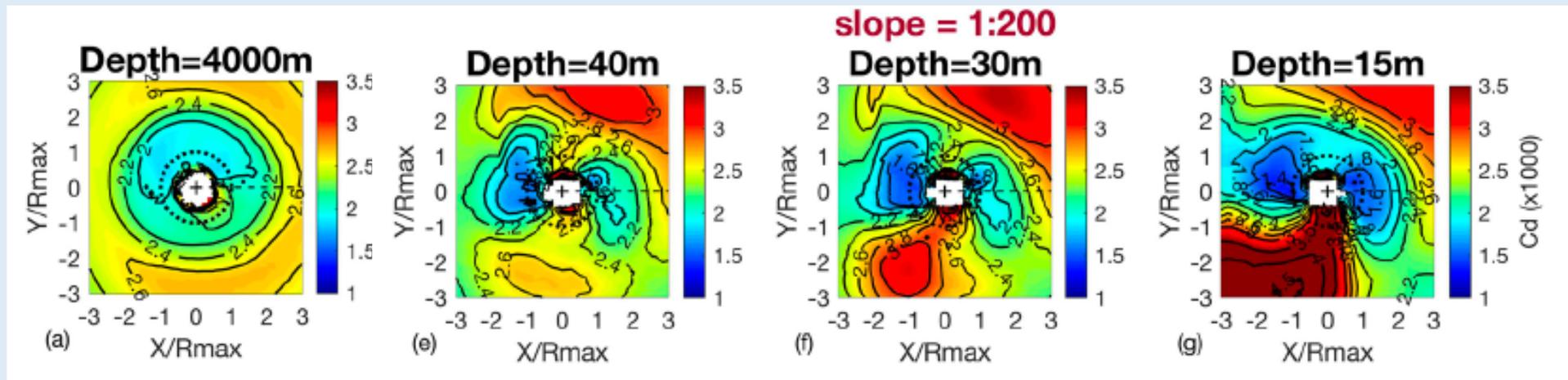
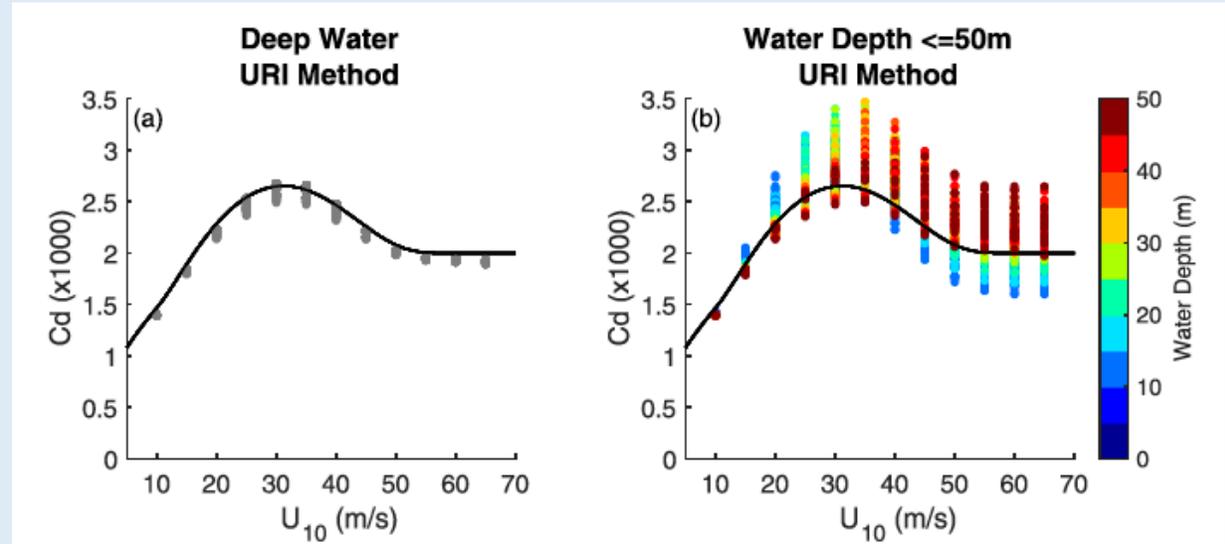
Dependence of  $C_d$  on misalignment angle  $\psi$  between wind and dominant waves

# Sea state dependence of $C_d$

Our recent modeling study suggests  $C_d$  strongly depends on sea states in coastal shallow waters (Chen et al. 2020a,b)

Right panels show that  $C_d$  under steady uniform wind significantly increases in shallow waters.

Bottom panels show how sea state dependence of  $C_d$  under tropical cyclones is enhanced in shallow waters.



## Sea state dependence of $C_\theta$ and $z_\theta$ ?

$$C_\theta = \left( \frac{1}{\kappa} \log \frac{10}{z_0} \right)^{-1} \left( \frac{0.74}{\kappa} \log \frac{10}{z_\theta} \right)^{-1}$$

Two key questions:

- If  $C_d$  and  $z_0$  are sea state dependent, are  $C_\theta$  and  $z_\theta$  also sea state dependent?
- Can the sea state dependence of  $z_\theta$  compensate (cancel) the sea state dependence of  $z_0$ , so that  $C_\theta$  remains sea state independent?

# Large eddy simulation (LES) of wind over a sinusoidal wave train

Surface wave length  $\lambda$ , wavenumber  $k = \frac{2\pi}{\lambda}$ , wave amplitude  $a$ , wave phase speed  $c$

Wave slope  $ka = 0.27$

LES domain size:  $5\lambda \times 5\lambda \times 2.4\lambda$ , LES grids:  $256 \times 256 \times 256$

Wind is driven by externally imposed horizontal pressure gradient

Weak heating from bottom for scalar flux simulations

Background surface roughness (due to unresolved small waves)  $z_{0b}$ ,  
 $kz_{0b} = 2.7 \times 10^{-3}$

Background surface roughness of scalar (due to unresolved small waves)  $z_{\theta b}$

We vary (relative) wind forcing ( $c/u_*$ ), wind direction, and  $z_{\theta b}$

## REFERNECES:

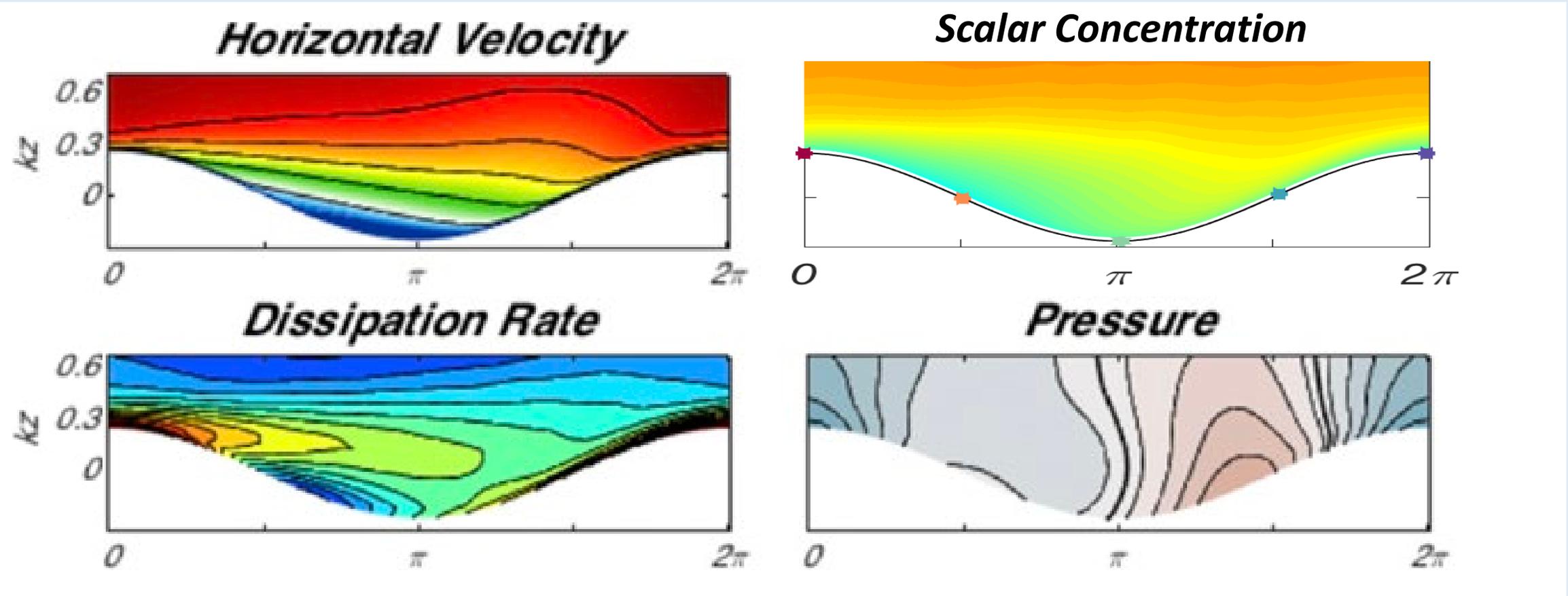
LES studies: Hara and Sullivan 2015; Sullivan et al. 2017; Husain et al. 2022a; 2022b

Validation of LES against laboratory observation: Husain et al. 2019

# Large eddy simulation (LES) of wind over a sinusoidal wave train

Phase averaged flow fields,  $c/u_* = 1.4$  (strongly wind forced).

WIND from Left to Right →

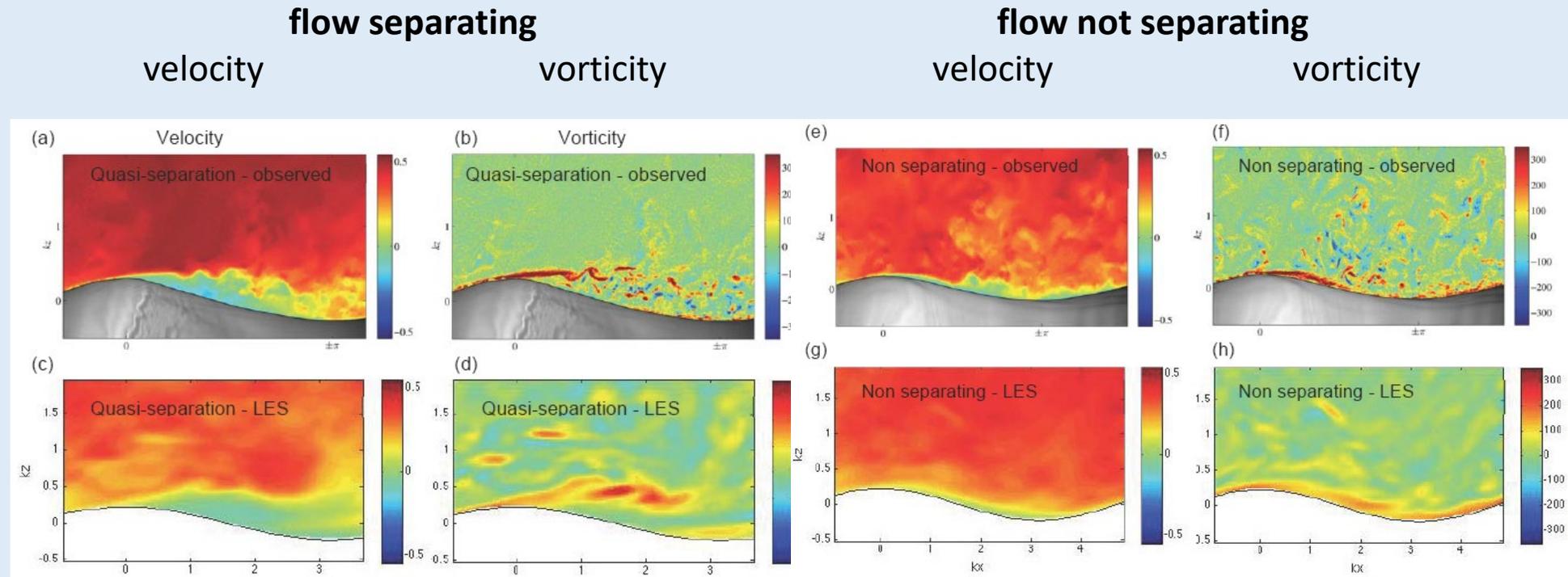


Behind the crest is a region of reduced wind speed, reduced turbulence, and reduced scalar concentration gradient.

# Airflow separation

Although we simulate conditions where the “ensemble averaged” flow field does not separate over a non-breaking wave train, instantaneous flow fields often show “separation like” patterns.

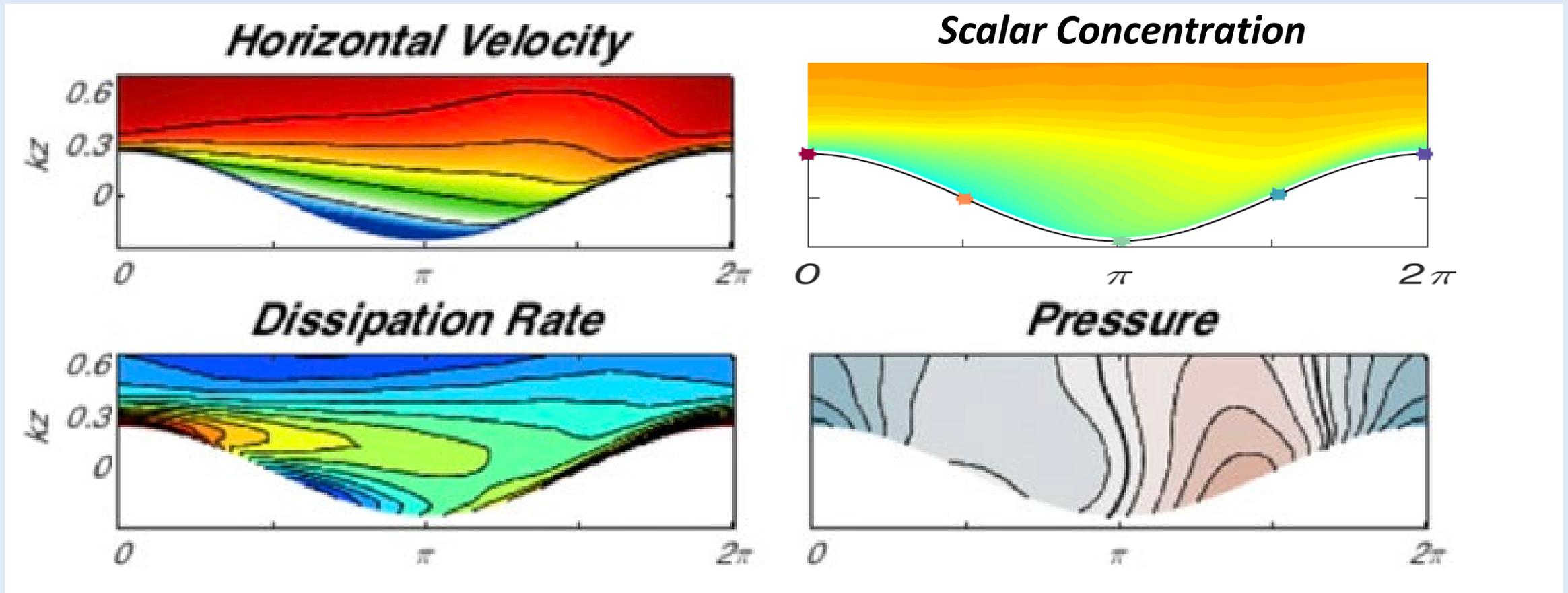
Our LES results are consistent with laboratory observations by Buckley and Veron (Univ. of Delaware).



Top: PIV observations, Bottom: LES results

# Large eddy simulation (LES) of wind over a sinusoidal wave train

Phase averaged flow fields

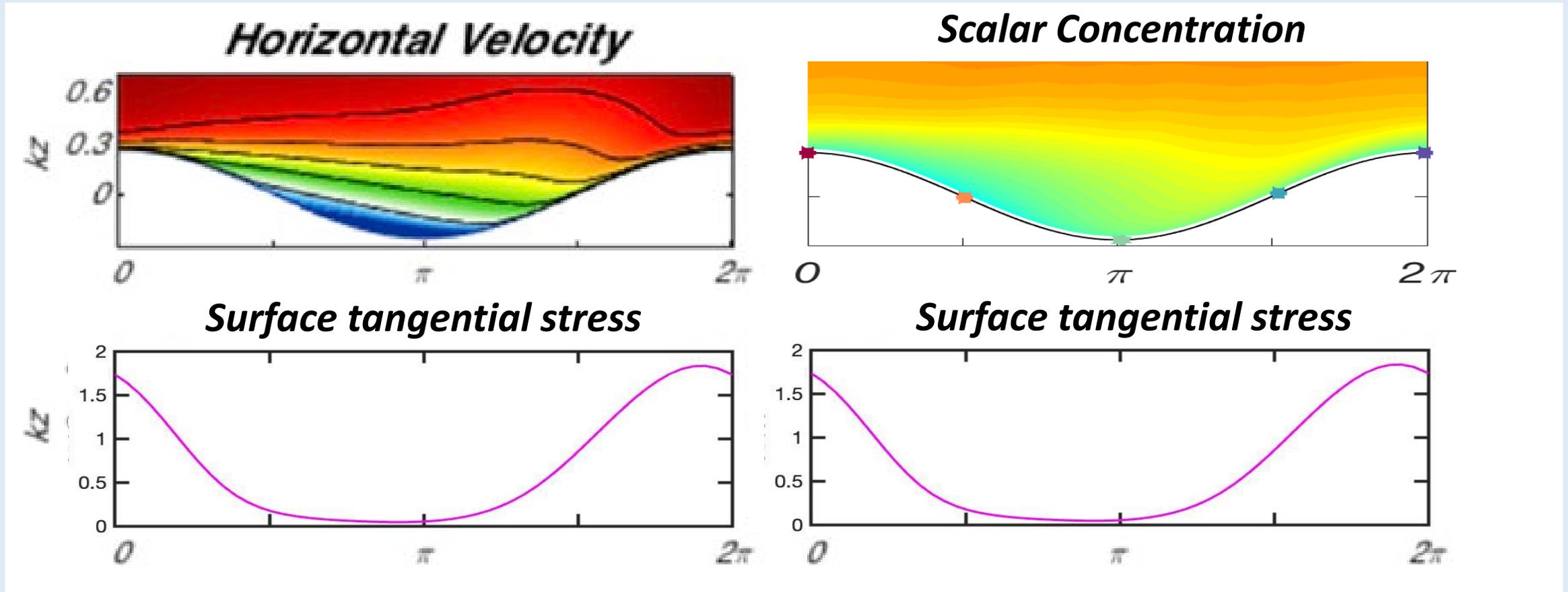


Airflow frequently separates from the crest.

Behind the crest is a region of reduced wind speed, reduced turbulence, and reduced scalar concentration gradient.

# Large eddy simulation (LES) of wind over a sinusoidal wave train

Phase averaged flow fields

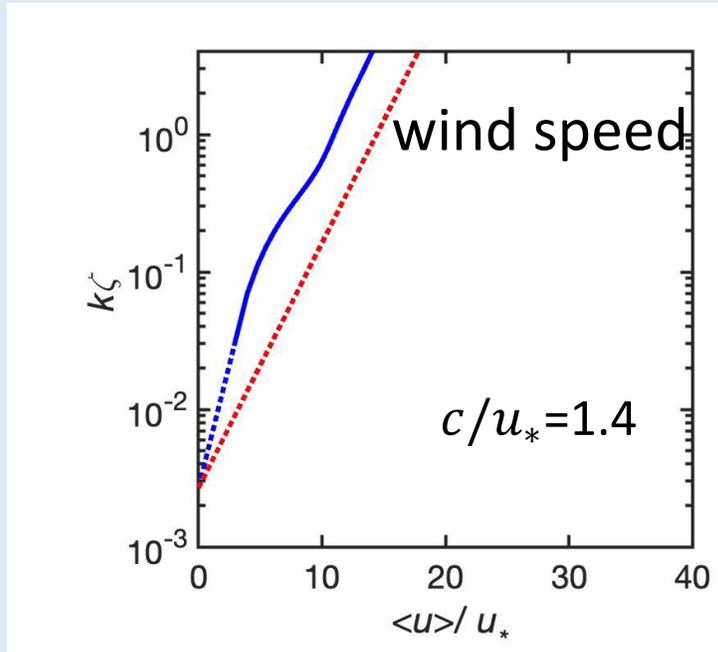


Airflow frequently separates from the crest.

Behind the crest is a region of reduced wind speed, reduced turbulence, and reduced scalar concentration gradient, **where the surface tangential stress becomes close to zero.**

Horizontally averaged analyses using a mapped vertical coordinate  $\zeta$  (Hara and Sullivan, 2015).

How are the mean wind speed profile  $\langle u(\zeta) \rangle$  modified from a flat surface to a wavy surface (if wind stress and scalar flux remain the same)?

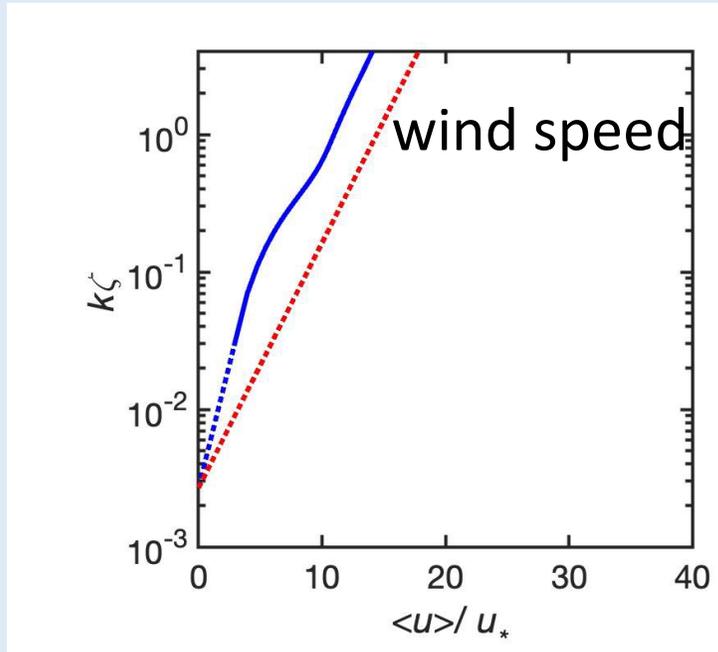


$\langle u \rangle$  over a wave train (blue) is shifted to the left of  $\langle u \rangle$  over a flat surface (red) away from the surface.

Roughness  $z_0$  increases over a wave train.

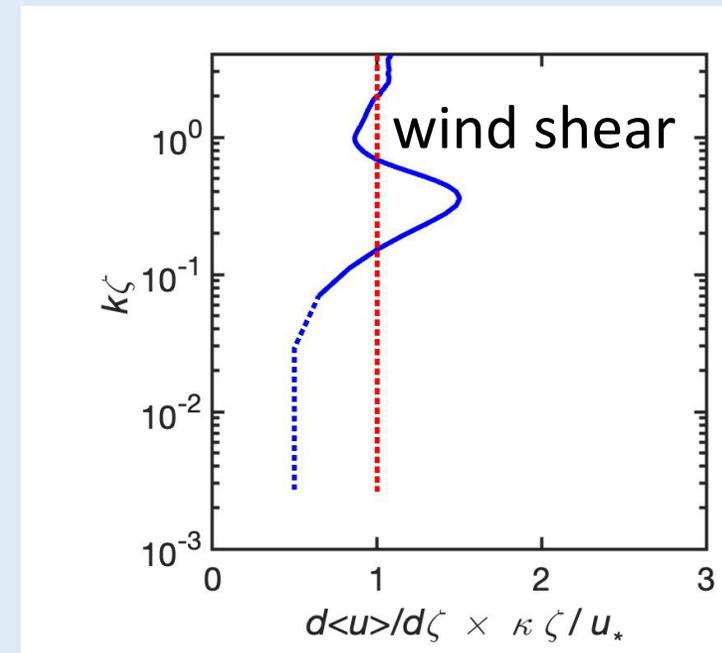
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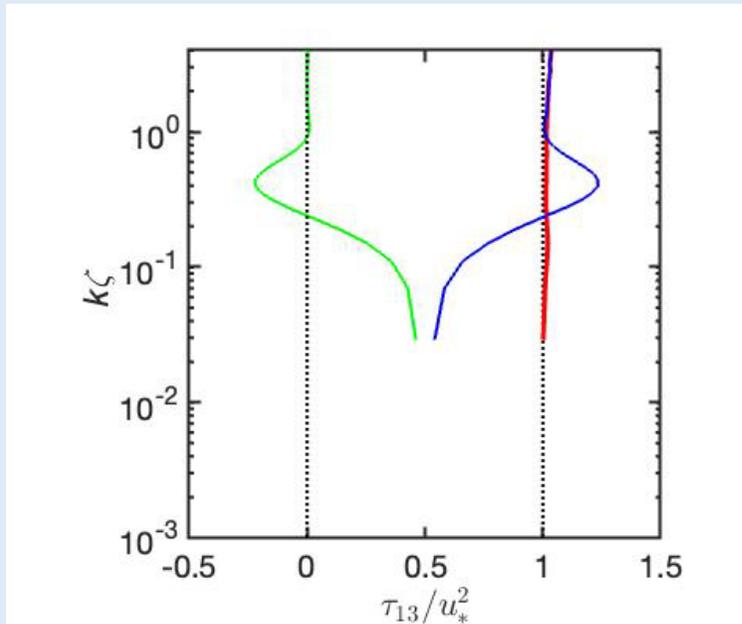


Wind shear is reduced over a wave train (blue) than over a flat surface (red) near the surface, hence,  $z_0$  increases.

Wind shear is enhanced near the height of wave crest. (Airflow separation makes the surface smoother?)

Horizontally averaged analyses using a mapped vertical coordinate  $\zeta$  (Hara and Sullivan, 2015).

How are the mean wind speed profile  $\langle u(\zeta) \rangle$  modified from a flat surface to a wavy surface (if wind stress and scalar flux remain the same)?



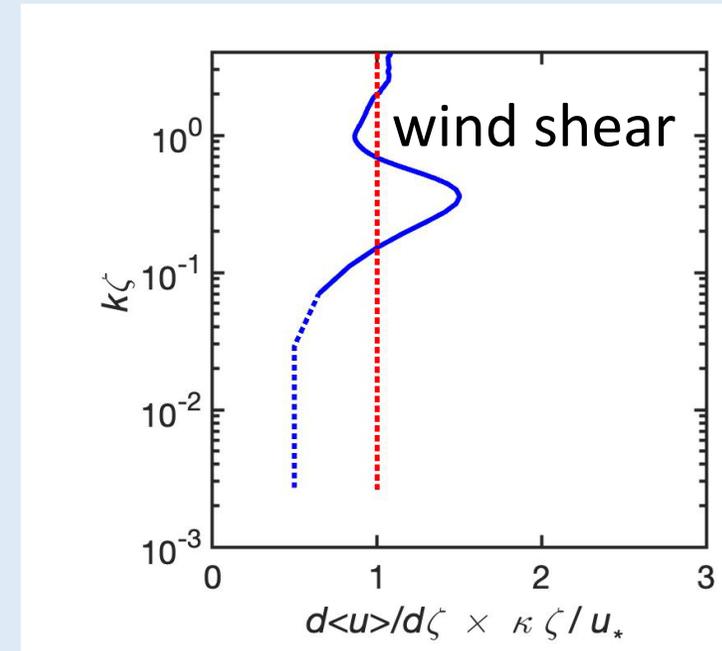
Momentum flux budget

Green: wave coherent stress

Blue: turbulent stress

Red: total stress

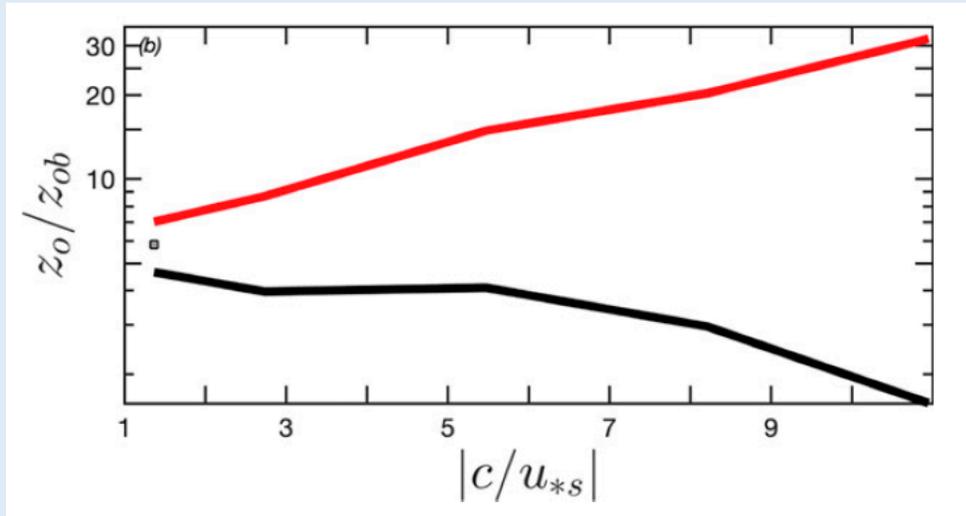
Turbulent stress is significantly reduced near the surface, causing the reduced wind shear.



Wind shear is reduced over a wave train (blue) than over a flat surface (red) near the surface, hence,  $z_0$  increases.

Wind shear is enhanced near the height of wave crest. (Airflow separation makes the surface smoother?)

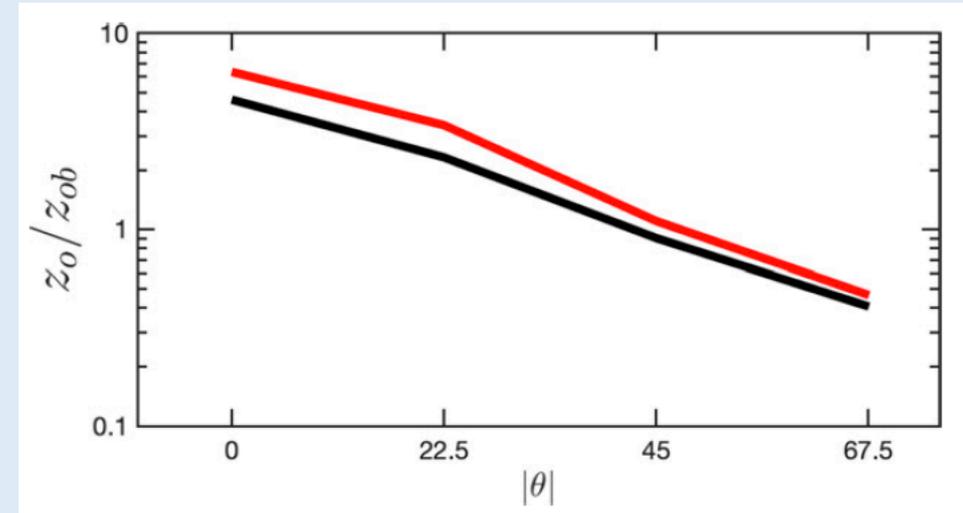
We may estimate  $z_0/z_{0b}$ , i.e., how much roughness has increased over a wave train compared to a flat surface. (Husain et al. 2022a,b)



← *strong wind*      *weak wind* →

With waves following wind (black), roughness is more enhanced with stronger wind forcing.

With wave opposing wind (red), roughness is more enhanced with weaker wind forcing.

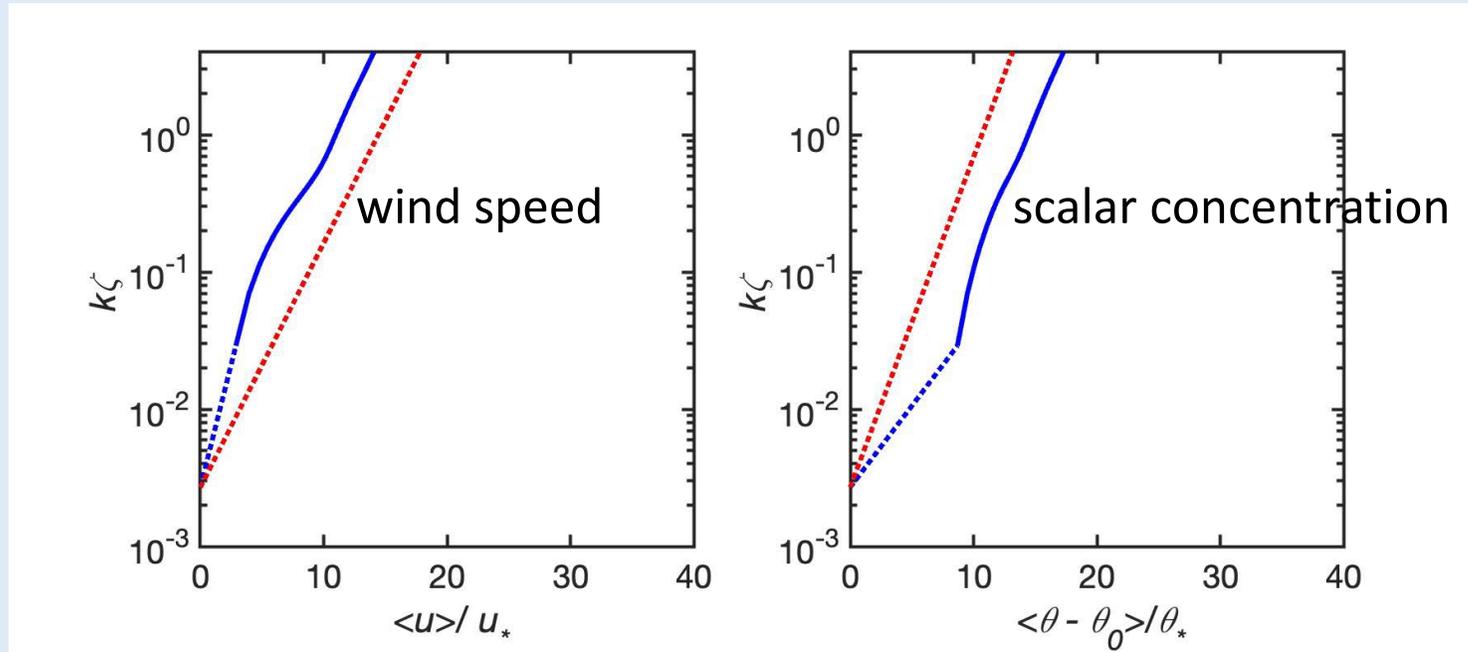


*wind and wave misaligned* →

If wave direction is close to wind direction, roughness is enhanced.

If wave direction is misaligned from wind direction by more than 45 degrees, **roughness is reduced compared to a flat surface.**

How are the mean wind speed profile  $\langle u(\zeta) \rangle$  and mean scalar concentration profile  $\langle \theta(\zeta) \rangle$  modified from a flat surface to a wavy surface (if wind stress and scalar flux remain the same)?



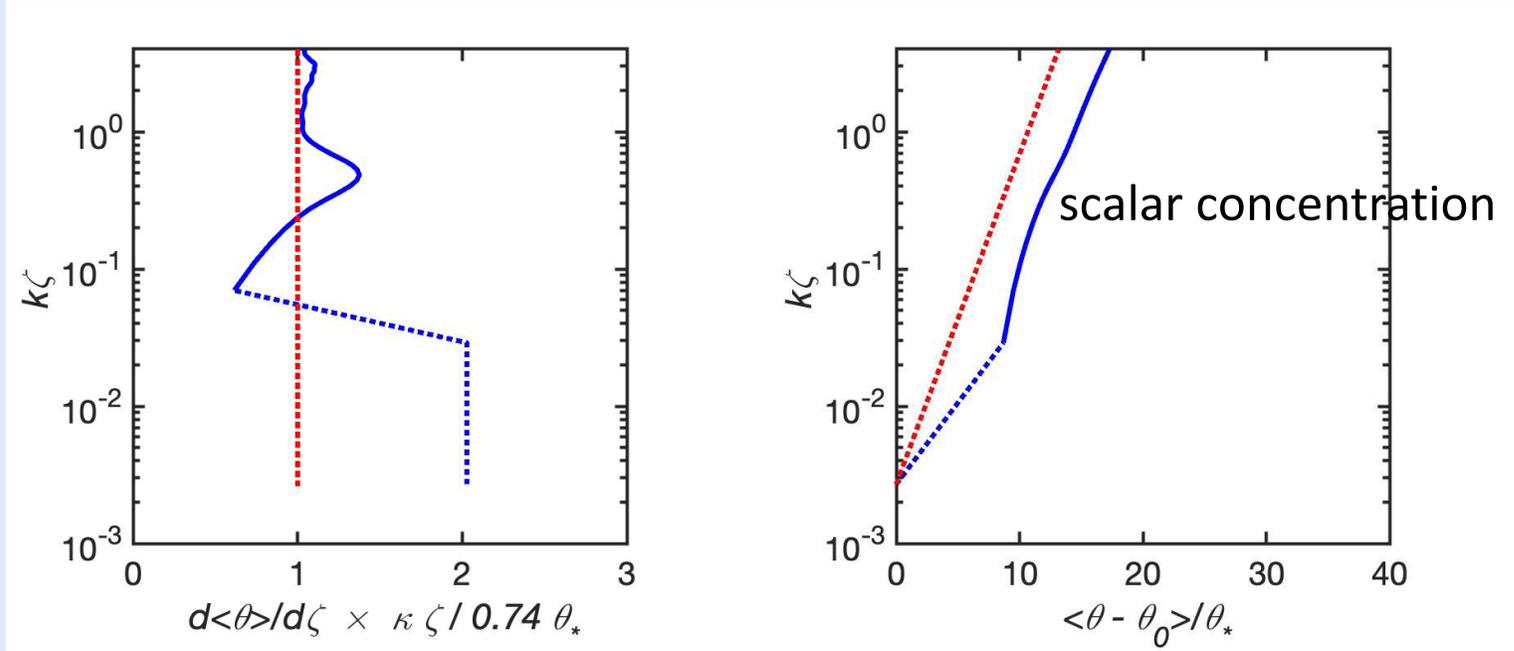
$\langle u \rangle$  over a wave train (blue) is shifted to the left of  $\langle u \rangle$  over a flat surface (red) away from the surface.

Roughness  $z_0$  has increased by a factor of  $\sim 5$ .  
 $C_d$  has increased by  $\sim 40\%$

$\langle \theta \rangle$  over a wave train (blue) is shifted to the right of  $\langle \theta \rangle$  over a flat surface (red) away from the surface.

Roughness  $z_\theta$  has decreased by a factor of  $\sim 5$ .  
 $C_\theta$  remains almost unchanged.

How are the mean wind speed profile  $\langle u(\zeta) \rangle$  and mean scalar concentration profile  $\langle \theta(\zeta) \rangle$  modified from a flat surface to a wavy surface (if wind stress and scalar flux remain the same)?

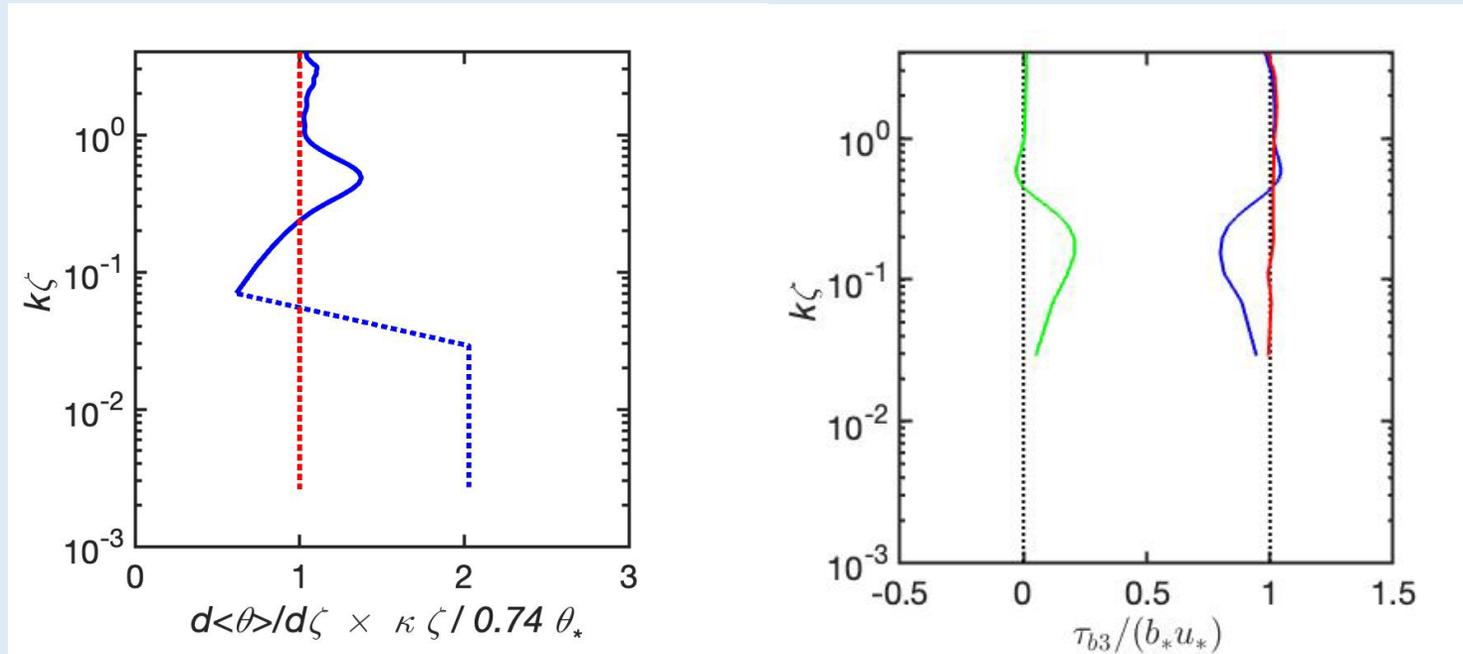


$\langle\theta\rangle$  is shifted to the left because the vertical gradient of  $\langle\theta\rangle$  is significantly enhanced near the surface.

$\langle\theta\rangle$  over a wave train (blue) is shifted to the left of  $\langle\theta\rangle$  over a flat surface (red) away from the surface.

Roughness  $z_\theta$  has decreased.

How are the mean wind speed profile  $\langle u(\zeta) \rangle$  and mean scalar concentration profile  $\langle \theta(\zeta) \rangle$  modified from a flat surface to a wavy surface (if wind stress and scalar flux remain the same)?



$\langle \theta \rangle$  is shifted to the left because the vertical gradient of  $\langle \theta \rangle$  is significantly enhanced near the surface.

Scalar flux budget

Green: wave coherent flux

Blue: turbulent flux

Red: total flux

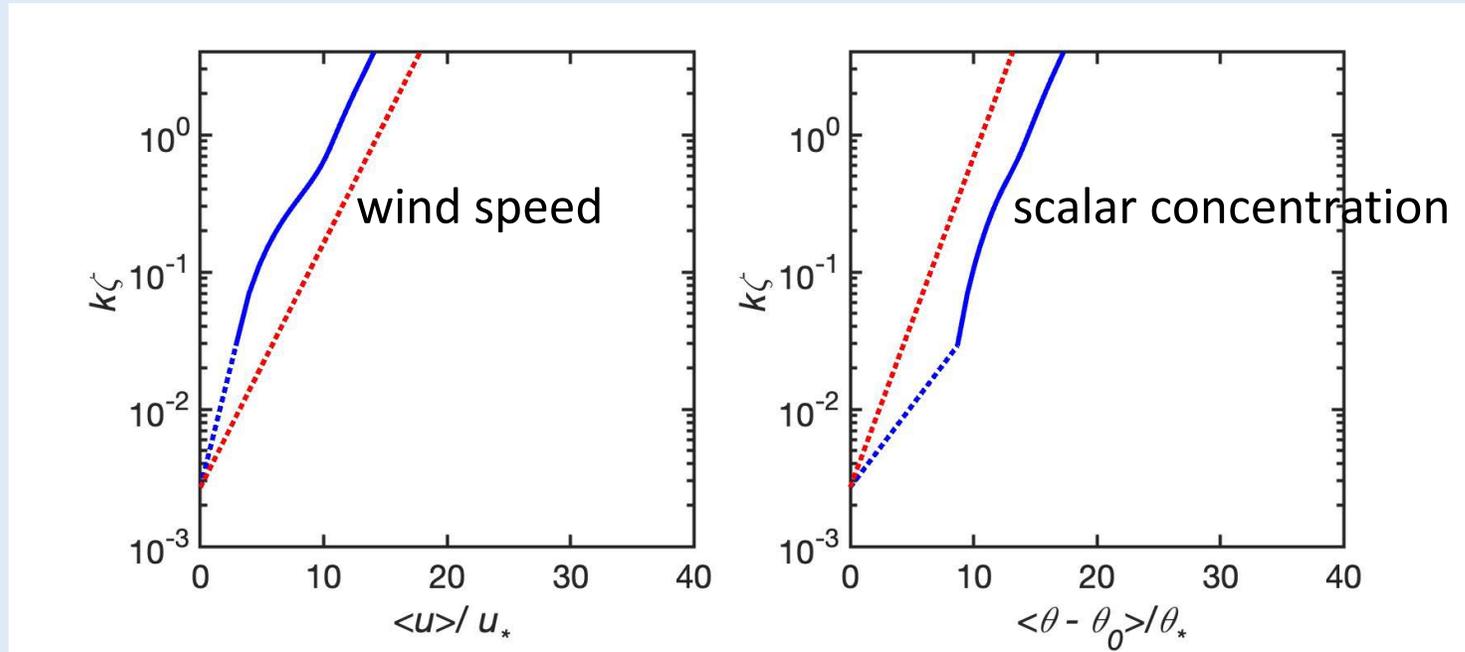
Turbulent scalar flux is not reduced near the surface.

But, turbulent stress is reduced near the surface.

Therefore, the vertical gradient of  $\langle \theta \rangle$  increases.

(Near the surface,  $u_*$  decreases but  $\theta_* u_*$  does not change. Therefore,  $\theta_*$  increases.)

How are the mean wind speed profile  $\langle u(\zeta) \rangle$  and mean scalar concentration profile  $\langle \theta(\zeta) \rangle$  modified from a flat surface to a wavy surface (if wind stress and scalar flux remain the same)?



$\langle u \rangle$  over a wave train (blue) is shifted to the left of  $\langle u \rangle$  over a flat surface (red) away from the surface.

Roughness  $z_0$  has increased.

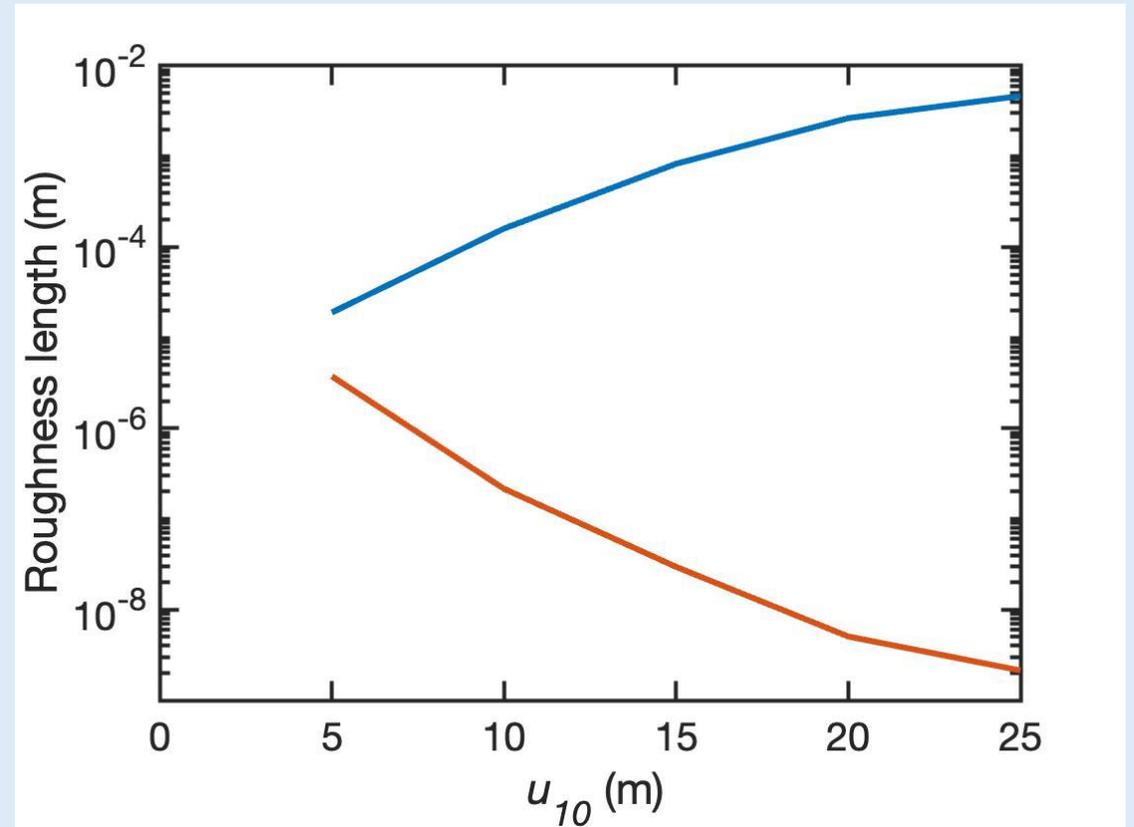
$\langle \theta \rangle$  over a wave train (blue) is shifted to the right of  $\langle \theta \rangle$  over a flat surface (red) away from the surface.

Roughness  $z_\theta$  has decreased.

Increase of  $z_0$  and decrease of  $z_\theta$  seem to (roughly) cancel each other, i.e.,  $C_\theta$  remains (roughly) unchanged, if the background roughness  $z_{0b}$  and  $z_{\theta b}$  are the same.

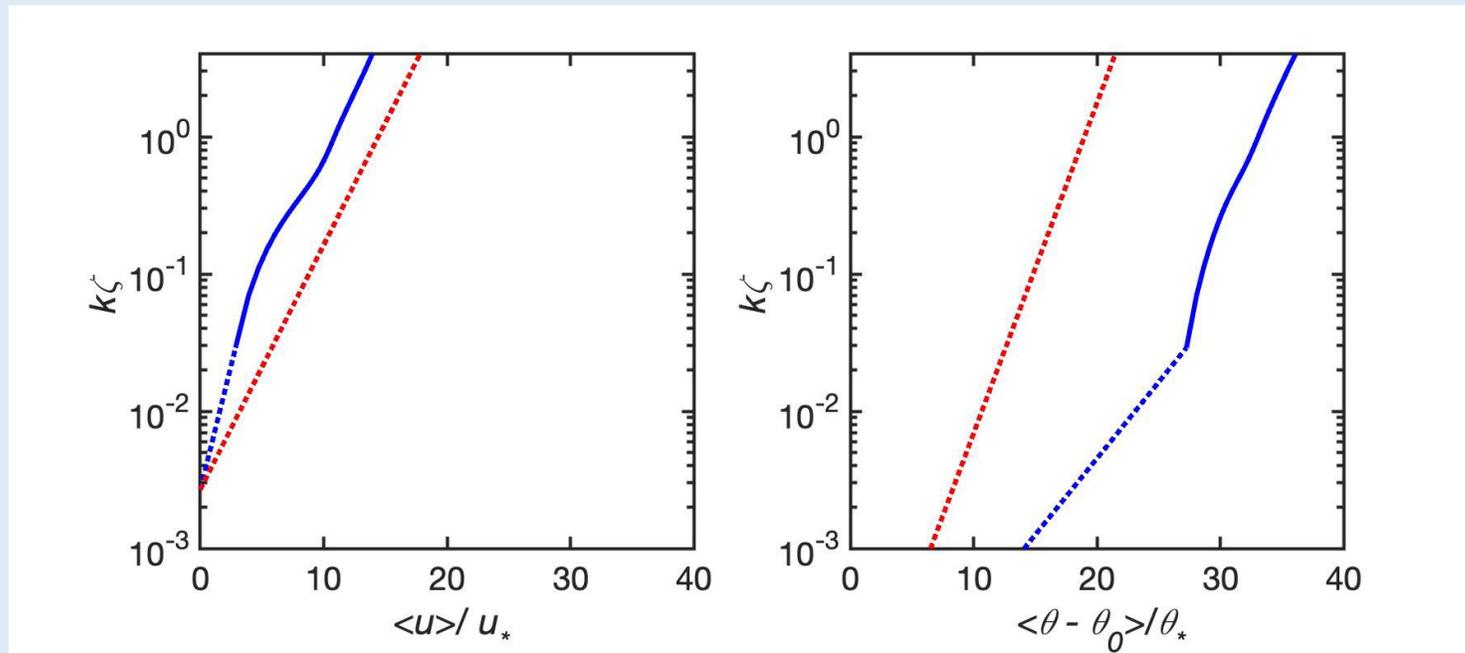
Recall that  $z_0$  is much larger than  $z_\theta$  except for very low wind speeds.

Therefore, the background roughness (due to unresolved small waves)  $z_{\theta b}$  should be much less than the background roughness  $z_{0b}$ .



$z_0$  (blue) and  $z_\theta$  (red) as functions of  $u_{10}$

We repeat the same LES experiment but reduces  $z_{\theta b}$  ( $z_{\theta b}/z_{0b} = 0.01$ ), which is more realistic.



Increase of  $z_0$  and decrease of  $z_\theta$  do not cancel each other, and  $C_\theta$  is significantly ( $\sim 20\%$ ) reduced by the waves, if the background roughness  $z_{\theta b}$  is much less than the background roughness  $z_{0b}$ .

## Conclusion:

- Scalar transfer coefficient  $C_\theta$  is a function of both  $z_0$  and  $z_\theta$ .
- Recent studies show that  $z_0$  can be strongly sea state dependent, particularly under tropical cyclones and in coastal shallow waters.
- Our LES study shows that  $z_0$  is significantly modified (usually increased) over a sinusoidal wave train (compared to a flat surface), depending on wind strength and direction. Airflow separations may play a significant role in modifying  $z_0$ .
- Our preliminary LES study shows that:
  - When  $z_0$  increases over a sinusoidal wave train (because the turbulent stress is reduced),  $z_\theta$  decreases (because the scalar flux is NOT reduced).
  - The effects of increasing  $z_0$  and decreasing  $z_\theta$  on  $C_\theta$  do not always cancel.  $C_\theta$  can be significantly reduced by waves.